

$$y = \tan^{-1}(x^2-1)^{\frac{1}{2}} + \csc^{-1} x \quad x > 1$$

$$y' = 2x \cdot \frac{1}{2}(x^2-1)^{-\frac{1}{2}} \cdot \frac{1}{1 + ((x^2-1)^{\frac{1}{2}})^2} + \frac{-1}{|x|\sqrt{x^2-1}}$$

$$= \frac{x}{\sqrt{x^2-1}} \cdot \frac{1}{x + (x^2-1)} - \frac{1}{|x|\sqrt{x^2-1}}$$

$$\frac{1}{x\sqrt{x^2-1}} - \frac{1}{x\sqrt{x^2-1}} = 0$$

Sep 28-9:28 AM

3.9a Derivatives of exponential functions

Sketch the derivative

$y = e^x$   
 $y' = e^x$

$$y' = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{e^{x+h} - e^x}{h}$$

$$\lim_{h \rightarrow 0} \frac{e^x \cdot e^h - e^x}{h} = \lim_{h \rightarrow 0} e^x \frac{e^h - 1}{h}$$

$y' = e^x$

Oct 5-7:24 PM

$$\boxed{\frac{d}{dx} e^x = e^x}$$

$$\frac{d}{dx} e^u = e^u \cdot \frac{du}{dx}$$

$$\boxed{\frac{d}{dx} e^u = \frac{du}{dx} \cdot e^u}$$

Sep 28-9:49 AM

Find  $dy/dx$  if

$$y = e^x \cdot e^{x^2}$$

$$y = e^{x+x^2}$$

$$y' = (1+2x) e^{x+x^2}$$

$$y = x^2 e^x - e^{\sqrt{3}x}$$

$$y' = x^2 \cdot e^x + 2x e^x - 3 \cdot \frac{1}{2}(\sqrt{3}x)^{-\frac{1}{2}} \cdot e^{\sqrt{3}x}$$

$$= x^2 e^x + 2x e^x - \frac{3e^{\sqrt{3}x}}{2\sqrt{3}x}$$

Oct 5-7:29 PM

The spread of the flu in a certain school is modeled by the equation

$$y = \frac{100}{1+e^{3-t}}$$

How fast is the flu spreading after 3 days?

$$y' = \frac{(1+e^{3-t}) \cdot 0 - 100 \cdot (-1) e^{3-t}}{(1+e^{3-t})^2} \Big|_{t=3}$$

$$= \frac{100 e^0}{(1+e^0)^2} = \frac{100}{2^2} = 25 \frac{\text{people}}{\text{day}}$$

on day 3 there are 25 new cases

Oct 5-7:45 PM

Derivative of  $y = a^x$

$$y = 2^x$$

$$y' = \ln 2 \cdot 2^x$$

$$\frac{d}{dx} a^u = \ln a \cdot a^u \cdot \frac{du}{dx}$$

Oct 5-7:33 PM

At what point on the graph of  $y = 2^t - 3$  does the tangent line have slope 21?

$$y' = 21$$

$$\ln 2 \cdot 2^t = 21 \quad t = 4.9$$

$$2^t = \frac{21}{\ln 2}$$

$$\sqrt{\ln 2}^t = \ln \frac{21}{\ln 2}$$

$$t \ln 2 = \ln \frac{21}{\ln 2}$$

$$t = \frac{\ln \left( \frac{21}{\ln 2} \right)}{\ln 2} \approx 4.9$$

Oct 5-7:34 PM

1.1 1.2 1.3 milk

A glass of cold milk from the refrigerator is left on the counter on a warm summer day. Its temperature  $y$  after sitting on the counter is  $y = 72 - 30 \cdot (0.98)^t$

Oct 5-7:36 PM